McKinley, T. D., Heinrich, K. J. F. \& Wittry, D. B. (1966). Proceedings of the First National Symposium on the Electron Microprobe, 1964. New York: John Wiley.
Miller, G. G. S. \& Black, P. J. (1970). Acta Cryst. A26, 527-532.
North, A. C. T. (1965). Acta Cryst. 18, 212-216.
Osawa, A. (1933). Sci. Rep. Tohoku Univ. 22, 803-823.
Parak, F., Mössbauer, R. L., Biebl, U., Formanek, H. \& Hoppe, W. (1971). Z. Phys. 244, 456-467.
Pearson, W. B. (1958). Handbook of Lattice Spacings and Structures of Metals and Alloys. p. 344. London: Pergamon Press.

Sikka, S. K. (1969). Acta Cryst. A 25, 396-397.
Singh, A. K. \& Ramaseshan, S. (1966). Acta Cryst. 21, 279-280.
Singh, A. K. \& Ramaseshan, S. (1968). Acta Cryst. B24, 35-39, 881.
Srinivasan, R. \& Сhacko, K. K. (1970). Z. Kristallogr. 131, 29-39.
Unangst, D., Muller, E., Müller, J. \& Keinert, B. (1967). Acta Cryst. 23, 898-901.

Wilson, A. J. C. (1942). Nature, Lond. 150, 151-152.
Wood, J. H. \& Pratt, G. W. (1957). Phys. Rev. 107, 9951001.

# The Crystal Structure of $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$ 

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The crystal structure of $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$ is tetragonal with $a=11.62$ (2) and $c=10.28$ (2) $\AA$. The space group is $I 4_{1} / a$ and $Z=4$. The Cs and Cl atoms are cubic close-packed and the Mn atoms are octahedrally coordinated by Cl atoms. Each $\mathrm{MnCl}_{6}$ octahedron is linked to six neighbouring octahedra by sharing five edges and one vertex.

## Introduction

The authors have recently completed a study of the crystal structures of compounds in the $\mathrm{CsCl}-\mathrm{MnCl}_{2}$ system and the crystal structure of $\mathrm{CsMnCl}_{3}$, which is related to that of $\mathrm{CsNiCl}_{3}$, has already been described (Goodyear \& Kennedy, 1973). The structures of $\mathrm{Cs}_{2} \mathrm{MnCl}_{4}$ and $\mathrm{Cs}_{3} \mathrm{MnCl}_{5}$ have been found to be similar to those of $\mathrm{Cs}_{2} \mathrm{MnBr}_{4}$ (Goodyear, Steigmann \& Kennedy, 1972) and $\mathrm{Cs}_{3} \mathrm{CoCl}_{5}$ (Powell \& Wells, 1935) respectively, and details of these will shortly be submitted for publication. $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$, however, is unique in that no other caesium complex halide of similar composition has previously been reported.

The material was prepared by heating a mixture, containing 4 molar parts of $\mathrm{MnCl}_{2}$ and 1 of CsCl , in an evacuated silica tube until molten and then cooling the specimen to room temperature at the rate of about $5^{\circ} / \mathrm{h}$. Red plate-like crystals were formed which were suitable for X-ray analysis. As was found with all the compounds in the series, the material was very hygroscopic and hence single crystals were examined and selected in a stream of dry nitrogen prior to mounting in sealed Lindemann-glass tubes. The density of the material was determined by weighing a sample quickly in air and in toluene.

## X-ray data

The unit-cell dimensions were determined from oscillation and Weissenberg photographs taken with $\mathrm{Cu} K \alpha$
radiation about an axis which turned out to be the $a$ axis. The symmetry was tetragonal and the observed density could be accounted for by assigning four molecules of $\mathrm{CsMn} \mathrm{Cl}_{9}$ to the unit cell. The complete crystal data are shown in Table 1.

## Table 1. Crystal data

Formula, $\mathrm{CsMn}_{4} \mathrm{Cl}_{9} ; \quad$ F.W. $671 \cdot 78$
Tetragonal; $\quad a=11 \cdot 62(2), c=10 \cdot 28$ (2) $\AA$
Mean $r(\mathrm{~cm}) . \quad Z=4, D_{o}=3 \cdot 26, D_{x}=3 \cdot 22 \mathrm{~g} \mathrm{~cm}^{-3}$
$\mu\left(\mathrm{cm}^{-1}\right): \quad 80 \cdot 3(\lambda=0.7107 \AA)$
Intensity data were collected from equi-inclination Weissenberg photographs taken about the $a$ axis with Mo $K \alpha$ radiation. The intensities of 417 reflexions, on layer lines 0 to 5 , were measured from multiple-film exposures using a Joyce-Loebl flying-spot microdensitometer; of these 318 were symmetrically independent. 118 reflexions were too weak to be observed.

The intensity data were corrected with the Lorentzpolarization factor and for absorption using the factors given by Bond (1959) for a cylindrical specimen. The observed reflexions satisfied the conditions $h+k+l=$ $2 n$ for $h k l, h=2 n$ for $h k 0$ and $l=4 n$ for $00 l$, which suggested $I 4_{1} / a$ (No. 88) as the only possible space group.

## Determination of the structure

The initial structure was determined from packing considerations and a knowledge of the space group.

Assuming typical values for ionic radii, the number of Cs and Cl atoms in the cell and the volume of the cell indicated that these atoms together formed a closepacked array. The relatively low $\mathrm{Cl} / \mathrm{Mn}$ ratio, $\frac{9}{4}$, suggested that the structure might consist of a threedimensional system of linked $\mathrm{MnCl}_{6}$ octahedra. Following Wells (1962), it was possible to see if this ratio was consistent with the linking of topologically equivalent octahedra in the space group $I 4_{1} / a$. In each octahedron let $p_{1} \mathrm{Cl}$ atoms be common to one octahedron, $p_{2}$ be common to two octahedra and in general $p_{n}$ be common to $n$ octahedra, then $\sum p_{n}=6$ and $\sum\left(p_{n} / n\right)=\frac{9}{4}$. There is just one solution of these equations which is consistent with the space group. With $p_{2}=2, p_{3}=3$ and $p_{4}=1$, the numbers of $p_{2}$-type, $p_{3}$-type and $p_{4}$-type Cl atoms in the cell would be 16, 16 and 4 respectively. Thus $p_{2}\left(p_{3}\right)$-type atoms could be placed at equipoint $16(f)$ and $p_{4}$-type at $4(a)$ or $4(b)$, leaving an equipoint of rank 4 available for the location of the Cs atoms.

The next step was to see if the unit-cell dimensions were simply related to those of the $\mathrm{MnCl}_{6}$ octahedron. In the structure of $\mathrm{CsMnCl}_{3}$ the average $\mathrm{Cl}-\mathrm{Cl}$ distance in the $\mathrm{MnCl}_{6}$ octahedra is $3.60 \AA$, so that the distance between opposite vertices is $5.09 \AA$. This is nearly equal to one half of the $c$ parameter of the unit cell of $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$, indicating that each octahedron might be so oriented in the cell that one of the fourfold axes of the octahedron is parallel to $\mathbf{c}$. If this is so it follows that the close-packed Cs and Cl atoms are distributed in a square array, of side $3 \cdot 60 \AA$, in planes perpendicular to $\mathbf{c}$, i.e. parallel to the $X Y$ plane. The remaining problem is to account for the $a$ parameter in terms of the square arrangement of Cs and Cl atoms. By choosing the outline of the unit cell as shown in Fig. 1, the $a$ parameter would be $\left(10 \times 3 \cdot 60^{2}\right)^{1 / 2}=11 \cdot 38 \AA$ which is sufficiently close to the observed value to support the argument so far.
If Cs atoms are located at the corners of the base of the cell and the octahedrally coordinated Mn atoms are inserted at the centres of those squares which have Cl atoms at the corners, then the layer shown in Fig. 1 has the composition $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$ and the cell would contain 4 such layers at heights $z=0, z=\frac{1}{4}, z=\frac{1}{2}$ and $z=\frac{3}{4}$. The relative orientation of these layers which is required by the space-group symmetry is also shown in Fig. 1. This proposed structure has Cs at equipoint $4(a), \mathrm{Mn}$ at $16(f)$, and Cl in two sets at $16(f)$ and one set at 4(b).

The model structure was tested by means of a twodimensional block-diagonal least-squares refinement using $0 k l$ data and assuming initial individual isotropic


Fig. 1. Square array of Cs and Cl atoms in a plane perpendicular to the $c$ axis. If Mn atoms are located at the centres of squares of Cl atoms, the whole layer has the composition $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$. The orientation of the layer at different heights in the unit cell is indicated.


Fig. 2. The outline of a primitive unit cell whose base is parallel to the close-packed layers of Cs and Cl atoms. The $Z^{\prime}$ coordinates are indicated as follows: $\mathrm{Cl}, Z^{\prime}=0 ; \mathrm{Cl}$. $\square \mathrm{Cs} Z^{\prime}=1 ; \mathbf{A n} Z=\frac{1}{2}$.

Table 2. Final atomic parameters
Origin is at $\overline{4}$. Standard deviations are given in parentheses.

|  | Equipoint | $x / a$ | $y / b$ | $z / c$ | $B\left(\AA^{2}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Cs | $4(a)$ | 0 | 0 | 0 | $2.97(12)$ |
| Mn | $16(f)$ | $0.2926(6)$ | $0.3950(7)$ | $0.0073(5)$ | $1.60(11)$ |
| $\mathrm{Cl}(1)$ | $16(f)$ | $0.1041(10)$ | $0.3021(10)$ | $-0.0060(10)$ | $1.64(17)$ |
| $\mathrm{Cl}(2)$ | $16(f)$ | $0.2097(9)$ | $0.5961(9)$ | $-0.0057(9)$ | $1.35(17)$ |
| $\mathrm{Cl}(3)$ | $4(b)$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 0 | $1.71(35)$ |

temperature factors of $2.5 \AA^{2}$ for Cs and $2.0 \AA^{2}$ for the other atoms．After one cycle of refinement the $R$ value， $\sum\left|\left|F_{o}\right|-\left|F_{c}\right|\right| / \sum\left|F_{o}\right|$ ，was $20 \%$ and this decreased to $7.3 \%$ after a further three cycles．The new atomic coordinates were then refired by the least－squares

Table 3．Magnitudes of observed and calculated structure factors on an absolute scale


Fig．3．The linking of the Cl atoms of one $\mathrm{MnCl}_{6}$ octahedron to the Mn atoms of neighbouring octahedra．Double lines indicate $\mathrm{Mn}-\mathrm{Cl}$ bonds；single lines the edges of the octa－ hedron．
method using all the available intensity data，and after 10 cycles $R$ was reduced to a minimum value of $9.6 \%$ and the calculated structure factor of each unobserved reflexion was less than the minimum observable value． In the final cycle of refinement，the shift in each posi－ tional parameter was less than $\frac{1}{25}$ and that in each thermal parameter less than $\frac{1}{12}$ of one standard devia－ tion．For the structure－factor calculations the atomic scattering factors for $\mathrm{Cs}^{+}, \mathrm{Mn}^{2+}$ and $\mathrm{Cl}^{-}$were taken from International Tables for X－ray Crystallography （1962）and interlayer scaling was achieved by scaling the observed to the calculated structure factors．

The final atomic parameters are given in Table 2 and the magnitudes of the observed and calculated struc－ ture factors are compared in Table 3.

## Description of the structure

The close packing of the Cs and Cl atoms is of the cubic variety．The indices of the close－packed planes are（132）and Fig． 2 shows a primitive cell whose base is parallel to these planes．The most interesting feature of the structure is the linking of symmetrically equiv－ alent octahedra to form a three－dimensional complex． $\mathrm{Cl}(1), \mathrm{Cl}(2)$ and $\mathrm{Cl}(3)$ atoms are in contact with 2 Mn ， 3 Mn and 4 Mn atoms respectively，so that each octahedron shares five edges and one vertex with six neighbouring octahedra．This arrangement is shown in Fig． 3.

Bond lengths and angles are listed in Table 4．The average lengths of the $\mathrm{Mn}-\mathrm{Cl}, \mathrm{Cl}-\mathrm{Cl}$ and $\mathrm{Cs}-\mathrm{Cl}$ bonds are $2.54,3.58$ and $3.72 \AA$ respectively and agree within $\pm 0.02 \AA$ with the corresponding distances in the $\mathrm{CsMnCl}_{3}$ structure．Because of the mutual repul－ sions of neighbouring Mn ions，the five shared edges are all shorter（ $3.447-3 \cdot 554 \AA$ ）than the seven unshared edges $(3.611-3.673 \AA)$ of the octahedron．The disposi－

Table 4．Bond lengths and angles
Standard deviations，attributable to e．s．d．＇s in the positional and cell parameters，are given in parentheses．

| Cl oct | dron |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{Mn}-\mathrm{Cl}\left(1^{\text {i }}\right.$ ） | 2.446 （14）$\AA$ | $\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {i }}\right.$ ） 2 | 2.532 （14）$\AA$ |
| $\mathrm{Mn}-\mathrm{Cl}\left(1^{*}\right)$ | $2 \cdot 436$（12） | $\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {ii }}\right) \quad 2$ | 2.511 （14） |
| $\mathrm{Mn}-\mathrm{Cl}(3)$ | 2.702 （9） | $\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {V }}\right.$ ） 2 | $2 \cdot 589$（12） |
| $\mathrm{Cl}\left(1^{\mathrm{i}}\right)-\mathrm{Cl}\left(2^{\text {i }}\right.$ ） | $3 \cdot 630$（17） | $\mathrm{Cl}\left(1^{1}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {i }}\right.$ ） | 93.7 （4）${ }^{\circ}$ |
| $\mathrm{Cl}\left(1^{\mathrm{i}}\right)-\mathrm{Cl}\left(2^{\text {ii }}\right)$ | $3 \cdot 647$（17） | $\mathrm{Cl}\left(1^{\mathrm{i}}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {ij }}\right.$ ） | 94.7 （4） |
| $\mathrm{Cl}\left(2^{i}\right)-\mathrm{Cl}(3)$ | $3 \cdot 554$（12） | $\mathrm{Cl}\left(2^{1}\right)-\mathrm{Mn}-\mathrm{Cl}(3)$ | 85.5 （3） |
| $\mathrm{Cl}\left(2^{i 1}\right)-\mathrm{Cl}(3)$ | $3 \cdot 554$（12） | $\mathrm{Cl}\left(2^{\text {i }}\right)-\mathrm{Mn}-\mathrm{Cl}(3)$ | 85.9 （3） |
| $\mathrm{Cl}\left(1^{v}\right)-\mathrm{Cl}\left(1^{i}\right)$ | $3 \cdot 617$（12） | $\mathrm{Cl}\left(1^{v}\right)-\mathrm{Mn}-\mathrm{Cl}\left(1^{\text {i }}\right.$ ） | $95 \cdot 6$（4） |
| $\mathrm{Cl}\left(1^{v}\right)-\mathrm{Cl}\left(2^{i}\right)$ | $3 \cdot 627$（16） | $\mathrm{Cl}\left(1^{*}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {i }}\right.$ ） | $93 \cdot 8$（4） |
| $\mathrm{Cl}\left(1^{\nu}\right)-\mathrm{Cl}\left(2^{\text {ii }}\right)$ | $3 \cdot 476$（15） | $\mathrm{Cl}\left(1^{v}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {ii }}\right)$ | $89 \cdot 2$（4） |
| $\mathrm{Cl}\left(1^{v}\right)-\mathrm{Cl}(3)$ | $3 \cdot 611$（12） | $\mathrm{Cl}\left(1^{5}\right)-\mathrm{Mn}-\mathrm{Cl}(3)$ | $89 \cdot 2$（3） |
| $\mathrm{Cl}\left(2^{\nu}\right)-\mathrm{Cl}\left(1^{\text {i }}\right.$ ） | $3 \cdot 476$（15） | $\mathrm{Cl}\left(2^{2}\right)-\mathrm{Mn}-\mathrm{Cl}\left(1^{\text {i }}\right.$ ） | $87 \cdot 3$（4） |
| $\mathrm{Cl}\left(2^{v}\right)-\mathrm{Cl}\left(2^{1}\right)$ | $3 \cdot 447$（20） | $\mathrm{Cl}\left(2^{2}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {i }}\right.$ ） | 84.7 （4） |
| $\mathrm{Cl}\left(2^{\nu}\right)-\mathrm{Cl}\left(2^{\text {ii }}\right)$ | $3 \cdot 666$（12） | $\mathrm{Cl}\left(2^{\text {® }}\right)-\mathrm{Mn}-\mathrm{Cl}\left(2^{\text {ii }}\right)$ | 91.9 （4） |
| $\mathrm{Cl}\left(2^{v}\right)-\mathrm{Cl}(3)$ | $3 \cdot 673$（11） | $\mathrm{Cl}\left(2^{\nu}\right)-\mathrm{Mn}-\mathrm{Cl}(3)$ | 87.9 （3） |
| $\mathrm{Cs}-\mathrm{Cl}$ distances |  |  |  |
| $\mathrm{Cs}-\mathrm{Cl}\left(1^{\text {i，ii，iin，iv }}\right)$ |  | $3 \cdot 698$（12） |  |
|  |  |  |  |
| $\begin{aligned} & \mathrm{Cs}-\mathrm{Cl}\left(1^{\mathrm{vi}, \mathrm{viin}_{1, v i n, i x}}\right) \\ & \mathrm{Cs}-\mathrm{Cl}\left(2^{1 \mathrm{in}, \mathrm{v}, v i, v i i}\right) \end{aligned}$ |  | $3 \cdot 755$（11） |  |

Table 4 (cont.)

| Idealized positions of atoms |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cs at Cl at | $(0,0,0)$ |  | Mn | at $(0 \cdot 3,0 \cdot 4,0)$ |  |  | $z=-\frac{1}{4}$ |  |
|  | $z=0$ |  |  | $z=\frac{1}{4}$ |  |  |  |  |
|  | $x$ | $y$ |  | $x$ | $y$ |  | $x$ | $y$ |
| (1) | $0 \cdot 1$ | $0 \cdot 3$ | $\left(1^{v}\right)$ | $0 \cdot 3$ | 0.4 | (1 $1^{\text {viii }}$ ) | $0 \cdot 2$ | $0 \cdot 1$ |
| (1ii) | $-0 \cdot 3$ | $0 \cdot 1$ | (11) | $-0 \cdot 1$ | $0 \cdot 2$ | (1 ${ }^{\text {ix }}$ ) | $-0.2$ | $-0 \cdot 1$ |
| (1ii) | $-0 \cdot 1$ | $-0 \cdot 3$ | (1 ${ }^{\text {vii }}$ ) | $0 \cdot 1$ | $-0.2$ | ( $2^{\text {v }}$ ) | $0 \cdot 3$ | $0 \cdot 4$ |
| (1 ${ }^{\text {iv }}$ ) | $0 \cdot 3$ | $-0.1$ | $\left(2^{\text {iii }}\right.$ ) | $0 \cdot 2$ | $0 \cdot 1$ | $\left(2^{\text {vi }}\right.$ ) | $-0 \cdot 1$ | $0 \cdot 2$ |
| (2) | $0 \cdot 2$ | 0.6 | ( $2^{\text {iv }}$ ) | $-0.2$ | $-0 \cdot 1$ | ( $2^{\text {vii }}$ ) | $0 \cdot 1$ | $-0 \cdot 2$ |
| (2 ${ }^{\text {ii }}$ ) | $0 \cdot 4$ | $0 \cdot 2$ |  |  |  |  |  |  |
| (3) | $0 \cdot 5$ | $0 \cdot 5$ |  |  |  |  |  |  |

Table 5. Distortion of the $\mathrm{Cl}-\mathrm{Mn}-\mathrm{Cl}$ angle
Column (a): due to the contraction (or extension) of the $\mathrm{Cl}-\mathrm{Cl}$ bond Column (b): due to the displacement of the Mn ion

tion of the neighbouring Mn ions (see Fig. 3) suggests that in an octahedron the Mn ion would be repelled in a direction predominantly away from $\mathrm{Cl}(3)$ and somewhat towards the $\mathrm{Cl}\left(1^{\mathrm{i}}\right)-\mathrm{Cl}\left(1^{v}\right)$ edge. This explains the very long $\mathrm{Mn}-\mathrm{Cl}(3)$ and the relatively long $\mathrm{Mn}-\mathrm{Cl}\left(2^{v}\right)$ bonds, and to some extent the wide variation in the shared $\mathrm{Cl}-\mathrm{Cl}$ distances.

The magnitudes of the $\mathrm{Cl}-\mathrm{Mn}-\mathrm{Cl}$ angles of the octahedron can best be accounted for by considering separately departures from the ideal value of $90^{\circ}$ due to (a) the contraction (or extension) of the $\mathrm{Cl}-\mathrm{Cl}$ edge and (b) the displacement of the Mn ion from the centre of the octahedron. These distortions, which are listed in Table 5, were calculated by assuming a constant $\mathrm{Mn}-\mathrm{Cl}$ distance of $2.536 \AA$ in case (a) and a constant $\mathrm{Cl}-\mathrm{Cl}$ distance of $3.582 \AA$ in case (b).

Finally all attempts at preparing the compound $\mathrm{CsMn}_{4} \mathrm{Br}_{9}$ failed. Although trigonally distorted $\mathrm{MnBr}_{6}$ octahedra are found in the structure of $\mathrm{CsMnBr}_{3}$ (Goodyear \& Kennedy, 1972), it appears that the $\mathrm{Mn}^{2+}$ ion is not large enough to be in contact with six $\mathrm{Br}^{-}$ ions at the vertices of an octahedron which is distorted
similarly to the $\mathrm{MnCl}_{6}$ octahedron found in the $\mathrm{CsMn}_{4} \mathrm{Cl}_{9}$ structure.

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## References

Bond, W. L. (1959). Acta Cryst. 12, 375-381.
Goodyear, J. \& Kennedy, D. J. (1972). Acta Cryst. B28, 1640-1641.
Goodyear, J. \& Kennedy, D. J. (1973). Acta Cryst. B29, 744-748.
Goodyear, J., Steigmann, G. A. \& Kennedy, D. J. (1972). Acta Cryst. B28, 1231-1233.

International Tables for X-ray Crystallography (1962). Vol. III. Birmingham: Kynoch Press.

Powell, H. M. \& Wells, A. F. (1935). J. Chem. Soc. pp. 359-362.
Wells, A. F. (1962). Structural Inorganic Chemistry, 3rd ed. Oxford: Clarendon Press.

